

# Estimates of Technology and Convergence: Simulation Results.

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June 2004

## **Abstract**

Using a Solow-Swan model with a stochastic saving rate and stochastic productivity we analyse the distributions of parameter estimates that emerge under various choices of technology, and of the dimension of the panel on which cross-section regressions are based. There are distinct asymmetries that characterize these distributions. These asymmetries become more pronounced when the effects of a near-unit root in the productivity shock become magnified over a longer time horizon and when the underlying production function is not Cobb-Douglas. Consequently, relying on traditional econometric transformations of these parameter estimates based on symmetric distributions, such as  $t$ -ratios, will be quite misleading if one tries to assess technology parameters and  $\beta$ -convergence.

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\*The first author gratefully acknowledges the hospitality of the Economics Department at the University of Guelph. Thanks also to Steve Dowrick, Timothy Kam, and participants at the Australasian Macro Workshop for helpful comments.

# 1 Introduction

In recent times researchers have made intensive use of cross-country evidence to assess alternative growth models. A central part of this research agenda concerns the empirical implications of different theories for the dynamic adjustment of per capita incomes. That these models converge to their country-specific steady state growth paths means that, in terms of the empirical growth literature, they satisfy conditional  $\beta$ -convergence<sup>1</sup>. Within the class of neoclassical growth models, however, the robustness of the conclusions of the empirical growth literature is coming under increasing scrutiny. Most recent criticism is centered around the choice of variables with which to characterise the steady-state growth path, or around the choice of estimation procedure. This paper is relevant to the second of these issues. Our approach is to revisit some of the early and influential empirical work which applies ordinary least squares to estimate technology parameters and convergence speed – our contribution being to apply these techniques to artificial data generated from a stochastic Solow-Swan model. This approach allows us to investigate the distributions of the parameters of interest.

There is a well-known theoretical literature on stochastic growth models. Mirman (1972, 1973) established the existence of steady-state distributions of the capital-labour ratio for a discrete-time model in which the productivity shock is either i.i.d. or follows a first-order Markov process. In Mirman's work, the support for these disturbances is the positive real line. Merton (1975) analyses a continuous-time version of the same model, except that randomness comes in through the rate of population growth. He derives steady-state probability distributions of a number important variables such as the capital-labour ratio, the output-labour ratio, the capital-output ratio, and the interest rate. He also shows the biases of the steady-state expected values compared with steady-state certainty equivalent estimates. Binder and Pesaran (1999) is cast in discrete-

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<sup>1</sup>There is a variety of terminology with respect to  $\beta$ -convergence. We follow that used by Durlauf and Quah (1999).

time and extends Mirman's results by allowing for stochastic disturbances to both the rate of technical change and the rate of population growth. They allow for unit roots in these processes, and also extend the support for the processes to include negative realisations subject to a lower bound. Curiously (given the observed empirical variability of the saving ratio) there appears to be no theoretical literature dealing with steady-state distributions of variables (or ratios of variables) in the Solow-Swan model in situations where, in addition to stochastic productivity and population growth, there is a stochastic saving rate.

The work most closely related to ours is that of Lee, Pesaran and Smith (1997). They examine properties of estimates of  $\beta$ -convergence obtained using a now-common cross-section approach (described in more detail in following sections) in which observations on each country in the panel are averaged over the time interval  $T$ , but the initial level of output is included in the OLS regression to capture dynamics. Each of the  $R$  countries in the sample shares a common Cobb-Douglas technology but is subject to individual stochastic processes for productivity and the labour supply. They derive an expression for the asymptotic  $R$ , small  $T$  bias in the estimate of  $\beta$ -convergence.

Our paper extends the work of Lee, Pesaran and Smith (1997) in several ways. Unlike them, we rely on a Monte Carlo investigation of the underlying Solow-Swan growth model with stochastic productivity and savings rates in order to consider the small  $R$ , small  $T$  case. This situation is perhaps more relevant in empirical work where the assumption of a common technology is most naturally applied to, say, the OECD countries in which case  $R$  is about 30. As we show later, this is much less than is required to justify reliance on asymptotic -  $R$  results. We also allow for a stochastic saving rate and investigate the effects of departures from Cobb-Douglas technology. Finally, we report features of the distribution of the estimated capital share parameter as well as the measure of  $\beta$ -convergence - it is the latter which is the primary focus of Lee, Pesaran and Smith (1997).

The rest of the paper is structured as follows. The next section briefly reviews

the derivation of the convergence-estimation framework used in the empirical growth literature. In section 3 we specify the stochastic closed economy Solow-Swan model with added disturbances to the rate of productivity growth and the saving rate, and in the following section we discuss the distributions of the parameter estimates of the capital share and convergence parameters as they emerge from the synthetic data. Finally we conclude.

## 2 Estimation of Convergence

In the closed economy Solow-Swan model the key equation governing dynamics is the proportionate rate of capital accumulation which is given by

$$\frac{d \log \tilde{k}}{dt} = s \frac{f(\tilde{k})}{\tilde{k}} - (\delta + n + \mu) \quad (1)$$

where  $f(\tilde{k})$  denotes a constant returns to scale production technology satisfying the Inada conditions written with  $\tilde{k}$ , the capital stock per effective worker, as its argument. The parameters  $s, \delta, n$  and  $\mu$  denote the saving rate, the depreciation rate, the population growth rate, and the rate of Harrod-neutral technical change. Log-linearising this expression gives the approximation

$$\frac{d \log \tilde{k}}{dt} \cong s \left[ \frac{d(f(\tilde{k})/\tilde{k})}{d\tilde{k}} \frac{d\tilde{k}}{d \log \tilde{k}} \right]_{\tilde{k}=\tilde{k}^*} (\log \tilde{k} - \log \tilde{k}^*). \quad (2)$$

If the production technology is Cobb-Douglas with capital share  $\alpha$ , (2) may be re-written as

$$\frac{d \log \tilde{k}}{dt} = s \left[ \alpha \tilde{k}^{\alpha-1} - \tilde{k}^{\alpha} \tilde{k}^{-1} \right]_{\tilde{k}=\tilde{k}^*} (\log \tilde{k} - \log \tilde{k}^*) \quad (3)$$

$$= s(\alpha - 1) \frac{f(\tilde{k}^*)}{\tilde{k}^*} (\log \tilde{k} - \log \tilde{k}^*) \quad (4)$$

$$= s(\alpha - 1) \frac{\delta + n + \mu}{s} (\log \tilde{k} - \log \tilde{k}^*) \quad (5)$$

$$= \beta (\log \tilde{k} - \log \tilde{k}^*) \quad (6)$$

where  $\beta = -(1 - \alpha)(\delta + n + \mu)$ . Substituting for  $\tilde{y} = \tilde{k}^\alpha$  yields

$$\frac{d \log \tilde{y}}{dt} = \beta (\log \tilde{y} - \log \tilde{y}^*). \quad (7)$$

By assuming nonstochastic productivity growth, Cellini (1997) transforms (7) into

$$\frac{d \log y}{dt} = c + \beta (\log y - \log y^*) \quad (8)$$

which may be regarded as an error correction mechanism if  $y$  and  $y^*$  are I(1) variables. Estimating a value of  $-1 < \hat{\beta} < 0$  is consistent with conditional  $\beta$  convergence, which is to say that output per worker (and output per effective worker, given the assumed constancy of productivity growth) converges to its steady state value at rate  $\beta$ . Because  $y^*$  and  $\tilde{y}^*$  depend on country-specific factors, this property is known as conditional  $\beta$  convergence.

A more popular approach, and the one which is the starting point for this paper, has been to note that (7) implies

$$\log \tilde{y}(t) - \log \tilde{y}^* = \exp^{\beta t} (\log \tilde{y}(0) - \log \tilde{y}^*) \quad (9)$$

where, again,  $\beta$  is the rate of convergence. The next step is to parameterise  $\tilde{y}^*$ ; in the Solow-Swan model with Cobb-Douglas technology, Mankiw, Romer and Weil (1992) have exploited the fact that this can be done explicitly since the steady state value of output per effective worker is given by

$$\log \tilde{y}^* = \frac{\alpha}{1-\alpha} \log \left( \frac{s}{\delta + n + \mu} \right). \quad (10)$$

Output per worker and output per effective worker are related by

$$\log y(t) = \log \tilde{y}(t) + \log A(t), \quad (11)$$

so (9) can be rewritten as

$$\begin{aligned} & \log y(t+H) - \log y(t) \\ = & \gamma_1 + \gamma_2 \left( \frac{\alpha}{1-\alpha} \log s - \frac{\alpha}{1-\alpha} \log(n + \delta + \mu) - \log y(t) \right) \end{aligned} \quad (12)$$

where  $\gamma_2 = 1 - \exp \beta H$  and  $\gamma_1 = (t + H - t \exp \beta H) \mu + \gamma_2 \log A(0)$ <sup>2</sup>. Equation (12) is the basis for the estimation of convergence speed in Mankiw, Romer and Weil (1992).

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<sup>2</sup>See Durlauf and Quah (1999), p.256.

### 3 The Simulation Model

The discrete-time specification of the model is as follows. Output is given by a constant returns production function with Harrod-neutral technical progress and, in the case of Cobb-Douglas production, satisfying Inada conditions. The rate of capital accumulation is determined by saving at (stochastic) rate  $s$ , and (deterministic) depreciation at rate  $\delta$ . Effective labour input  $E$  is made up of a stochastic productivity term  $A$  and deterministic stock of labour  $N$ . The initial labour force is normalised to unity. Basic equations of the model are as follows, with country subscripts ( $j$ ) suppressed. The production technology, restricted to be constant-returns CES, is

$$Y_t = F(K_{t-1}, E_{t-1}), \quad (13)$$

while capital depreciates at rate  $\delta$

$$K_t = s_t Y_t + (1 - \delta) K_{t-1}, \quad (14)$$

and the labour force grows at rate  $n$ ,

$$E_t = A_t N_t, \quad N_t = \exp(n't). \quad (15)$$

where  $n' = \ln(1 + n)$ . In a cross-section of OECD countries the saving rate lies between 15.8% for Mexico and 33.9% for Finland; in individual countries  $s$  appears to show positive serial correlation. As is usual in this literature, the saving rate is proxied by the investment share in GDP. We assume the process for  $s$  to be

$$s_t = s + \theta_t, \quad \theta_t = \rho_s \theta_{t-1} + \epsilon_{s,t}, \quad 0 \leq \rho_s \leq 1 \quad (16)$$

where  $\epsilon_{s,t}$  is  $N(0, \sigma_s^2)$ <sup>3</sup>. Since it is implicit that this is a single-commodity model, there is no reason to constrain the saving rate to be positive.

The productivity shock is given as

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<sup>3</sup>Binder and Pesaran (1999) assume that the distribution of shocks is truncated on the left, to exclude large negative shocks. Although our simulations assume normality, there was not a single case of shocks being 'too large' in the sense of inducing a negative level of output.

$$A_t = \exp(\mu' t + \varsigma_t), \quad \varsigma_t = \rho_A \varsigma_{t-1} + \epsilon_t, \quad 0 \leq \rho_A \leq 1, \quad (17)$$

where, again  $\mu' = \ln(1 + \mu)$  is the mean growth rate, and  $\epsilon'_{A,t}$  is  $N(0, \sigma_A^2)$ . Note that the literature assumes that the productivity shock to be typically very persistent. In the following simulations we will do the same.

The deterministic component of the above model is assumed to be the same for all countries in the sample, reflecting the usual assumption that all countries have access to a common technology. In the case analysed in this paper we assume, for simplicity, that commonality of deterministic components also implies that population growth rates are the same across countries. In the empirical growth literature, OECD countries are often considered to be homogeneous in terms of technology, and this motivates the initial choice of 30 as the number of countries used in the simulations. We also let this number increase to 120 and examine the effect that such an increase will have on the resulting distributions of the parameter estimates. Starting from the same initial point, each 'country' is simulated for  $H$  periods, and observations between  $t = 70$  and  $t = H$  are retained as data for estimation. The unrestricted 'Barro regression' is

$$\ln(Y_{j,H}/N_{j,H}) - \ln(Y_{j,70}/N_{j,70}) = \beta_0 + \beta_1 \ln s_j + \beta_2 \ln(Y_{j,70}/N_{j,70}) + \epsilon_j \quad (18)$$

where  $s_j$  is the sample-mean saving rate for country  $j$ . The interpretation of  $\beta_1$  and  $\beta_2$  is usually motivated from the result of the previous section, where production is taken to be Cobb-Douglas with capital exponent  $\alpha$ . In Mankiw, Romer and Weil (1992) the only stochastic element in the model is the initial condition  $Y_{j,70}/N_{j,70}$  which is assumed to be independent of the cross-sectional disturbance term. In particular  $\mu$ ,  $\delta$  and  $n$  are nonstochastic and, on the common-technology assumption,  $\mu$  and  $\delta$  are the same across countries. Following Mankiw, Romer and Weil (1992) in ignoring the variability implied by the inclusion of the sample mean  $\mu_j$  in the expression for  $\beta$ , an estimate of the conditional convergence parameter  $\beta$  and technology parameter  $\alpha$  can be obtained from (19) and (20) where

$$\beta_1 = \frac{\alpha}{1 - \alpha} (1 - \exp(\beta[H - 70])) \text{ and} \quad (19)$$

$$\beta_2 = \exp(\beta[H - 70]) - 1 \tag{20}$$

Although the objective of this paper is to revisit results obtained in the OLS framework used by Mankiw, Romer and Weil (1992) and many others subsequently, we recognise that the use of OLS estimates  $\hat{\beta}_1$  and  $\hat{\beta}_2$  to obtain estimates of  $\alpha$  and  $\beta$  is problematic. There are several issues. The deterministic model of the previous section implies a restriction on estimation of  $\beta_1$  and  $\beta_2$ , encapsulated in (19) and (20). Imposition of this restriction would also require that cross-sectional variation in  $\mu'_j$ , as in (17) be taken into account<sup>4</sup>. Further, it follows from the setup of this section that measurement error is induced by taking sample means of the saving rate and the productivity growth rate. Finally, it is clear that the assumption (maintained by Mankiw, Romer and Weil (1992) and others) that the regressors are independent of the disturbance term is *not* valid in the present setup. Our simulation framework, which is intended to be a literal interpretation of the Solow-Swan model with common (stochastic) technology and stochastic saving, generates cross-sectional variation in the initial condition  $Y_{j,70}/N_{j,70}$  from a prior history of productivity and saving shocks. Since these shocks have persistence, sample-period values of  $s$  and  $\mu$  from  $t = 70$  to  $H$  are correlated with the initial condition and with the disturbance term.

## 4 Simulation Results

Our simulation results are based on parameter choices that are consistent with stylized facts. They are  $s_0 = 0.25$ ,  $\alpha = 0.333333$ ,  $n = 0.02$ ,  $\delta = 0.04$ ,  $\mu = 0.02$ ,  $\sigma_s^2 = 0.02$ ,  $\sigma_A^2 = 0.02$ ,  $\rho_s = 0.5$  and  $\rho_A = 0.95$ . We use a CES production function with different values for the elasticity of substitution parameter  $\sigma$ . At  $\sigma = 1$  we have the Cobb-Douglas function which is used in the discussion of convergence

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<sup>4</sup>With few exceptions (of which Lee, Pesaran and Smith (1997) is one), empirical work generally emphasises cross-sectional variation in sample population growth rather than in sample realisations of productivity but for simplicity we abstract from cross-sectional variation in population growth.

in section 2. It has been used explicitly in the Solow-Swan model of Makiw, Romer and Weil (1992) and offers the theoretical foundation of most empirical work in the literature. Table 1 presents the Cobb-Douglas analysis, while Table 2 that of a more general constant-returns CES for different values of  $\sigma$ . We define the period of analysis  $T$  as  $H - 70$  from the previous section.

The first row of Table 1 gives the simulation results for a group of 30 homogeneous countries over a 35 period horizon ( $R = 30, T = 35$ ) using 10,000 artificial data sets generated with the above parameter choices. This group for example may represent the OECD countries over the last 35 years. For each  $(R, T)$  combination we report the mean and the mean-squared error (MSE) and the mean absolute bias (MAB) of the estimated  $\alpha$  and  $\beta$  parameters as well as the proportion of times that the estimate of the convergence parameter  $\beta$  was undefined, when the solutions to equations (19) and (20) generate imaginary values. Even though the mean of the estimates is reasonably close to the true value of -0.0399 for  $\beta$ , this proportion is still problematically high at about 7 percent. Also the estimate of  $\alpha$  is not very close to the true value of  $1/3$  and its MSE is quite high. Things worsen considerably when  $T$  increases while  $R$  is fixed. In that case the effects of the near unit root in the productivity shock are magnified and they create not only imprecision in the way that the parameters are estimated, but also a dramatic increase in the proportion of ill-defined (imaginary) values of  $\beta$ . In fact when  $T = 100$  this proportion is nearly 50 percent and the distribution of the  $\beta$ -estimates is highly skewed to the right, irrespective of the number of countries  $R$ . For fixed values of  $T$ , on the other hand, as  $R$  increases the distribution of the estimates becomes more symmetric and tight and the MSE of the both  $\hat{\alpha}$  and  $\hat{\beta}$  decreases.

Hence, under the null hypothesis of a Cobb-Douglas production function that forms the basis of the analytical results of the previous section, we obtain a striking and at first hand disconcerting pattern of the shape of the distribution of the convergence parameter  $\beta$  and to a lesser extent of the capital share parameter  $\alpha$ . These tend to be quite skewed to the right and hence econometric results using standard statistics based on symmetry assumptions, such as

t-ratios will not be valid to assess statistical significance. However, the problem of evaluating convergence goes deeper than that. Even if we were to use robust econometric methods such as Least Absolute Deviation regression we would still run into similar problems (see the lower panel of Table 1 for examples). Standard regression estimates which underlie  $\beta$ -convergence, represent average behavior over time and ignore what happens to the whole distribution, see Quah (1996, 1997). In that case using robust methods, see Koenker and Basset (1978), Koenker (1982) and Buchinsky (1994), would not be of help, since these methods concentrate on what happens to specific parts of the distribution such as the median or specific quantiles. Consequently when testing for convergence one may want to look at methods that emphasize the use of distribution dynamics based on transition matrices and their continuous counterpart, stochastic kernels as in Quah (1997) or nonparametric density estimates of the growth rate distribution over time as in Bianchi (1997).

Table 2 presents the OLS results of the CES analysis with different choices of  $\sigma$  for a single pair ( $R = 30, T = 35$ ) and the same parameter choices as in Table 1 (the distribution parameter on capital,  $\omega$ , is set equal to one third). Clearly  $\sigma = 1$  replicates the Cobb-Douglas case, but as  $\sigma$  decreases the results deteriorate. As  $\sigma$  decreases the proportion of ill defined  $\beta$ 's increases and the distribution of the  $\beta$ -estimates becomes more skewed. Even small mis-specifications in the form of departures from Cobb-Douglas technology induce large changes in the estimate of  $\alpha$ , which in this case would be mistakenly identified with the capital share parameter in a Cobb-Douglas production function. Also the distribution of the  $\alpha$ -estimates becomes quite skewed and the MSE deteriorates dramatically. The results demonstrate that if Cobb-Douglas is not valid then the distribution shapes of the estimates for any given combination of  $R, T$  will become fairly skewed and reliance on standard symmetry based statistics will be quite problematic in any econometric analysis.

## 5 Conclusions

Using a Solow-Swan model for the case with a stochastic saving rate and stochastic productivity growth we analyze the distribution of parameter estimates that emerges under various parameter choices. The examination of the Monte Carlo distributions of the parameter estimates suggests that these parameter estimates cannot be used to assess  $\beta$ -convergence when combined with traditional econometric statistics that are based on symmetric distributions, such as  $t$ -ratios. There are distinct asymmetries that characterize these distributions which become more pronounced when the effects of a near-unit root in the productivity shock become more pronounced and when the underlying production function is not Cobb-Douglas. For the setup analysed here, the use of robust methods is not likely to overcome the estimation problems induced by these asymmetries.

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**Table 1** $\alpha = 1/3, \beta = -0.0399, \rho_A = 0.95, \rho_S = 0.5, N = 10,000$ 

$(R, T)$	$Mean(\hat{\alpha})$	$MSE(\hat{\alpha})$	$MAB(\hat{\alpha})$	$Mean(\hat{\beta})$	$MSE(\hat{\beta})$ ( $\times 10^{-4}$ )	$MAB(\hat{\beta})$ ( $\times 10^{-2}$ )	Prop. ill- defined $\hat{\beta}$
<b>OLS estimates</b>							
(30,35)	0.2698	4.773	0.3561	-0.0368	6.747	2.394	0.0668
(30,50)	0.3762	176.4	0.5630	-0.0283	6.809	2.939	0.2318
(30,100)	0.0581	647.2	1.352	-0.0118	10.78	4.145	0.4659
(60,35)	0.3324	0.0744	0.1446	-0.0384	4.625	1.913	0.0176
(60,50)	0.3252	5.438	0.1822	-0.0338	5.093	2.390	0.1278
(60,100)	0.2483	2.130	0.2723	-0.0142	8.609	3.910	0.4477
(120,35)	0.3528	0.0143	0.0926	-0.0376	3.521	1.690	0.0001
(120,50)	0.3328	0.0168	0.0979	-0.0379	3.908	1.905	0.0501
(120,100)	0.2973	0.0378	0.1329	-0.0163	6.937	3.710	0.4538
<b>LAD estimates</b>							
(30,35)	0.1421	88.57	0.7217	-0.0346	9.129	2.708	0.1076
(30,50)	0.2622	2196	1.641	-0.0251	0.888	3.197	0.2563
(30,100)	0.7601	817.8	1.727	-0.0107	12.17	4.253	0.4713

**Table 2**

$$\beta = -0.0399, \omega = 1/3, R = 30, T = 35, \rho_A = 0.95, \rho_S = 0.5, N = 10,000$$

$\sigma$	$Mean(\hat{\alpha})$	$MSE(\hat{\alpha})$	$MAB(\hat{\alpha})$	$Mean(\hat{\beta})$	$MSE(\hat{\beta})$ ( $\times 10^{-4}$ )	$MAB(\hat{\beta})$ ( $\times 10^{-2}$ )	Prop. ill- defined $\hat{\beta}$
1.00	0.2698	4.773	0.3561	-0.0368	6.747	2.394	0.0668
0.98	-0.0770	452.9	1.882	-0.0373	6.841	2.426	0.0775
0.95	-0.5219	17140.0	3.851	-0.0375	6.981	2.434	0.0805
0.90	0.3042	894.0	2.310	-0.0377	6.806	2.433	0.0870
0.80	0.6886	6541.0	3.797	-0.0384	6.886	2.452	0.0999
0.70	-0.2888	8951	3.820	-0.0390	7.060	2.484	0.1124